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## MATH221 05 problems Name, ID

1. Explain why all these statements are false.
(a) The complete solution is any linear combination of $x_{p}$ and $x_{n}$.
(b) A system $A x=b$ has at most one particular solution.
(c) The solution $x_{p}$ with all free variables zero is the shortest solution (minimum length $\|x\|)$. Find a conterexample.
(d) If $A$ is invertible there is no solution $x_{n}$ in the nullspace.
2. True or False.
(a) Any matrix has at least one pivot variable.
(b) An invertible matrix has no free variables.
(c) A square matrix has no free variables.
(d) An $m$ by $n$ matrix has no more than $n$ pivot variables.
(e) An $m$ by $n$ matrix no more than $m$ pivot variables.
