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**MATH221 02 problems**

Name, ID

1. It is impossible for a system of linear equations to have exactly two solutions. Explain Why.

2. True or false? Give a specific counterexample when false.

(a) If columns 1 and 3 of  $B$  are the same, so are columns 1 and 3 of  $AB$ .

(b) If rows 1 and 3 of  $B$  are the same, so are rows 1 and 3 of  $AB$ .

(c) If rows 1 and 3 of  $A$  are the same, so are rows 1 and 3 of  $AB$ .

(d)  $(AB)^2 = A^2B^2$ .

3. Explain these facts. If the third column of  $B$  is all zero, the third column of  $EB$  is all zero for any  $E$ . If the third row of  $B$  is all zero, the third row of  $EB$  might not be zero.

4. True or False and explain your answers.

(a) If  $A^2$  is defined then  $A$  is square.

(b) If  $AB$  and  $BA$  are defined then  $A$  and  $B$  are square.

(c) If  $AB$  and  $BA$  are defined then  $AB$  and  $BA$  are square.

(d) If  $AB = B$  then  $A = I$ .